

M.Sc. Statistics(Sem. -II) EXAMINATION -04-NOV-2017

Distribution Theory :PARER 2 , sub code-2753

TIME : ^{2.30}~~Two~~ Hours.

TOTAL MARKS:70

Note: (i) All Questions are Compulsory

(ii) All Full Questions carry equal marks.

1. (a) Let $f(x, y) = \begin{cases} 2, & \text{if } 0 \leq X \leq Y \leq 1 \\ 0, & \text{elsewhere} \end{cases}$ then derive 8
- (i) Marginal density of x.
- (ii) Marginal density of y.
- (iii) Conditional density of x given y.
- (iv) $E(X|Y = y)$
- (b) Let $X \sim \text{Poisson}(\lambda)$ then derive characteristic function of 6
X. Hence obtain its mean and variance.

OR

1. (a) Let the joint pdf of X and Y be given by: 6
- $$f_{x,y}(x, y) = \frac{1}{2\pi\sqrt{1-\rho^2}} \exp\left[-\frac{x^2 - 2\rho xy + y^2}{2(1-\rho^2)}\right] \text{ where } |\rho| < 1. \text{ Find}$$
- the marginal pdf of X and Y
- (b) Let the joint pdf be given by $f(x, y) = \lambda_1 \lambda_2 e^{-(\lambda_1 x + \lambda_2 y)}$ 8
- $0 < x < \infty, 0 < y < \infty$ obtain the marginal density of X
and Y also obtain the joint distribution function of X and
Y. Are X and Y independent?

2. (a) Define power series distribution. Show that first two 8
cumulants uniquely determine the power series
distribution.
- (b) Define NTA distributions. Define probability generating 6
functions of it ..Hence obtain its pdf

OR

2. (a) Define NTA and NTB distributions. Define probability generating functions of both distributions. 8
- (b) Derive recurrence relation for moments in the case of Poisson-Poisson distribution. 6
3. (a) State and prove Fisher-Cochran Theorem. 8
- (b) In usual notation, prove following result
 $G_3(z) = G_1(G_2(z))$

OR

- 3 (a) Define non-central chi-square random variable and obtain its probability distribution. 8
- (b) Define singular and non-singular multinomial distribution. Find mean, variance – covariance matrix of Multinomial Distribution. 6
4. (a) State the p.d.f of a Weibull distribution. If X has $W(X, \sigma, p)$ then derive the distribution of x^p . 6
- (b) Derive joint p.d.f. of r th & s th order statistics. 8

OR

4. (a) Derive Standard Error of r -th sample moment stating the necessary condition. 8
- (b) Derive p.d.f. of r th order statistics. 6
5. (a) State and prove two Property of non-central χ^2 distribution 8
- (b) Let $X \sim N(\mu, \sigma^2)$ and $Y \sim N\sigma^2 X^2(n)$ be two independent rv's. then derive the p.d.f. of $T = X/(Y/n)^{1/2}$. Give the name of the Statistic. 6

OR

- 5 (a) Derive the pdf of the r th order statistics based on the random sample of size n from exponential distribution with

mean θ .

- (b) Write a short note on non-central F-distribution.

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