

T.Y.B.Sc. EXAMINATION **OCT-2017**
M-303 ADVANCED NUMERICAL METHODS AND
DESCRETE MATHEMATICS - 8963

TIME:-3
HOURS

INSTRUCTIONS: (1) All questions are compulsory.
 (2) Each question carries equal marks

TOTAL MARKS:-100

- QUE. 1 A Apply Graffee's root squaring method to determine the approximate roots of the equation $x^3 - 7x^2 + 10x - 2 = 0$. 7M
 B Describe Muller's method. 7M
 C Describe Symmetric function of roots. 6M
- OR
- QUE. 1 A Describe Horner's method. 7M
 B Describe Lin-Bairstow's method. 7M
 C Use Ramanujan's method to find smallest root of equation $\sin = 1-x$. 6M
- QUE. 2 A Discuss Jacobi method of iteration 7M
 B Discuss method of Factorization. 7M
 C Solve the equation by gauss Jordan method 6M
 $x + 2y + z = 8, 2x + 3y + 4z = 20, 4x + 3y + 2z = 16$.
- OR
- QUE. 2 A Find inverse of matrix using Crout's Method. 7M

$$\begin{bmatrix} 1 & 2 & 3 \\ 3 & 2 & 1 \\ 2 & 1 & 3 \end{bmatrix}$$

 B Solve by seidel method of iteration the system 7M
 $8x - 3y + 2z = 20, 6x + 3y + 12z = 35$ and $4x + 11y - z = 33$.
 C Discuss Gauss elimination method. 6M
- QUE. 3 A Draw the Hasse diagram of (S_{60}, D) . 7M
 B If (P, \leq) is Poset, then (P, \geq) is also Poset. 7M
 C For set $S = \{2, 3, 6, 12, 24, 36\}$ prove that (S, D) is a Poset but not lattice. 6M
- OR
- QUE. 3 A If (P, R) is Poset, then (P, \tilde{R}) is also Poset, where \tilde{R} is converse relation of R. 7M
 B For $(a, b), (c, d) \in N \times N, (a, b) R (c, d) \Leftrightarrow ad = bc$. Prove that R is an equivalence relation on $N \times N$. Also find $[(3, 4)]$. 7M
 C Prove that (N, \leq) is a lattice, where $a \leq b \Leftrightarrow a$ is factor of b . 6M
- QUE. 4 A $(B, *, \oplus, ', 0, 1)$ is Boolean algebra $a, b \in B$ prove that 7M
 $a \leq b \Leftrightarrow a * b' = 0 \Leftrightarrow b' \leq a' \Leftrightarrow a' \oplus b = 1$.
 B State and prove distributive inequalities for lattice 7M
 C Define: Boolean isomorphism, atom of Boolean algebra, and find atoms of $(B, *, \oplus, ', 0, 1)$ where $B = S_{30}$ 6M

OR

- QUE. 4 A State and prove De-Morgan's laws in Boolean algebra. 7M
- B $(P(A), *, \oplus)$ is lattice where for $X, Y \in P(A)$ $X * Y = X \cap Y$ and $X \oplus Y = X \cup Y$ 7M
- C $(L, *, \oplus)$ is lattice for $a, b \in L$ $aRb \Leftrightarrow a \oplus b = b$ prove that R is equivalence relation on L. 6M
- QUE. 5 A $(B, *, \oplus, ', 0, 1)$ is Boolean algebra, for any $x_1, x_2 \in B$ 7M
- $A(x_1 * x_2) = A(x_1) \cap A(x_2)$
- B Prove : sum of all min-terms of n-variables X_1, \dots, X_n is 1 7M
- C Obtain sum of product canonical form of $\alpha(x_1, x_2, x_3) = x_1 x_2' + x_3$ 6M
- OR
- QUE. 5 A $(B, *, \oplus, ', 0, 1)$ is for Boolean algebra. for any $x_1, x_2 \in B$ 7M
- $A(x_1 \oplus x_2) = A(x_1) \cup A(x_2)$
- B $(B, *, \oplus, ', 0, 1)$ is Boolean algebra, for $x, y \in B$ prove that 7M
- $x \leq y \Leftrightarrow x * y' = 0 \Leftrightarrow y' \leq x' \Leftrightarrow x' \oplus y = 1.$
- C Obtain product of sum canonical form of $\alpha(x_1, x_2, x_3) = x_1 x_2 x_3.$ 6M