

INSTRUCTIONS (1) ALL QUESTIONS ARE COMPULSORY.
 (2) EACH QUESTION CARRY EQUAL MARKS.

Q.1 A Derive differentiation formula based on Newton's forward interpolation formula. [7]

B Obtain the value of $f'(90)$ using Stirling formula to the following data. [7]

x	60	75	90	105	120
f(x)	28.2	38.2	43.2	40.9	37.7

OR

Q.1 A Derive differentiation formula based on Stirling formula. [7]

B Find $y'(6)$ and $y''(6)$ from the following table. [7]

X	2	3	4	5	6	7
Y	4	8	15	7	6	2

Q.2 A Derive: Trapezoidal rule [7]

B Evaluate $\int_2^4 x^2 dx$ using Simpson's $\frac{1}{3}$ rule, where $h = 0.50$ [7]

OR

Q.2 A Derive Simpson's $\frac{3}{8}$ rule. [7]

B Find the approximate value of $\int_0^{\frac{\pi}{2}} \sin \theta d\theta$ by dividing the interval into six equal parts by Weddle's Rule [7]

Q.3 A Discuss symbol for integration formula [7]

B Evaluate $\int_0^1 x^2 + 1 dx$ correct upto three decimal places by Euler-Maclaurin's formula [7]

OR

Q.3 A Prove: $Q_{31}(1) = \frac{h}{24} \{-1, 13, 13, -1\}$ [7]

B Derive: $-Q_{22}(0)$ [7]

Q.4 A Derive Newton-Raphson formula. [7]

B using method of Iteration, Solve the equation: $f(x) = x^3 + x^2 - 1 = 0$ correct upto three decimal places. [7]

OR

Q.4 A Discuss: Bisection method. [7]

B Derive: The method of false position [7]

Q.5 A Given the differential equation for Runge-Kutta 2nd order $\frac{dy}{dx} = y + x$ with $y(0) = 1$, find $y(0.2)$ whenever $h = 0.1$. [7]

B Discuss Euler's method. [7]

OR

Q.5 A Discuss: Taylor's series method [7]

B Using Euler's modified method, solve $\frac{dy}{dx} = 2x^2 + y$, $y(0) = 1$, compute $y(0.1)$ and $y(0.2)$ whenever $h = 0.1$. [7]